

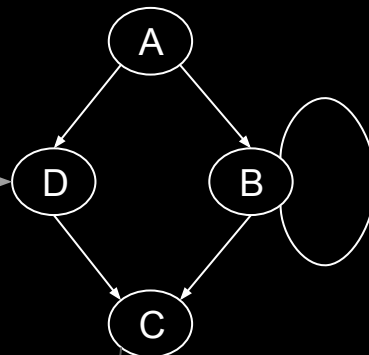
Streaming Process Mining

January 2025

<A, B, C>
<A, B, B, C>
<A, B, B, B, B, C>
<A, D, C>

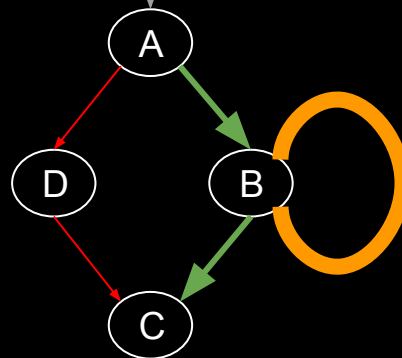
Event log
pre-processing

Process discovery



Enhancements

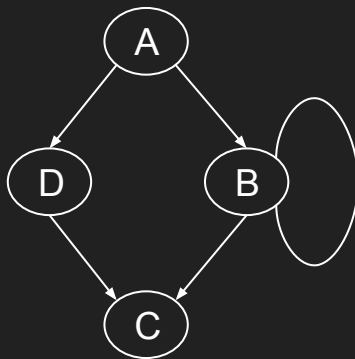
Conformance checking



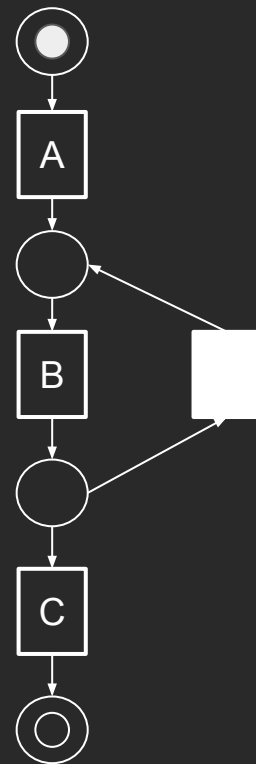
Initial event log

<A, B, C>
<A, B, B, C>
<A, B, B, B, B, C>
<A, D, C>

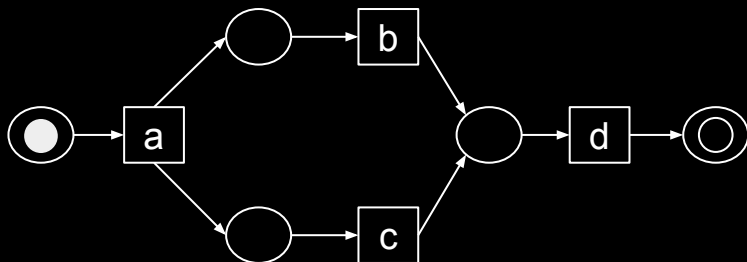
Discovered abstraction (i.e., directly-follows graph)



Discovered process model (i.e., Petri net, BPMN)



Petri nets



Definition 2.2 (Petri net, unlabelled Petri net). A Petri net over a given alphabet Σ is a tuple (P, T, A, M_0, F, l) consisting of:

- a set of places P ;
- a set of transitions T , such that $P \cap T = \emptyset$;
- a multiset arc relation $A \subseteq \mathbb{M}((P \times T) \cup (T \times P))$;
- an initial marking $m_0 \subseteq \mathbb{M}(P)$;
- a set of final markings F , being a set of multisets over P ;
- a partial labelling function $l: T \rightarrow \Sigma$.

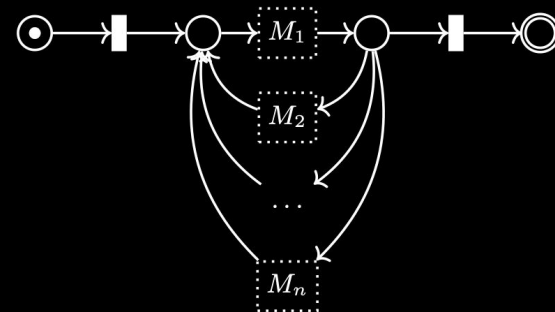
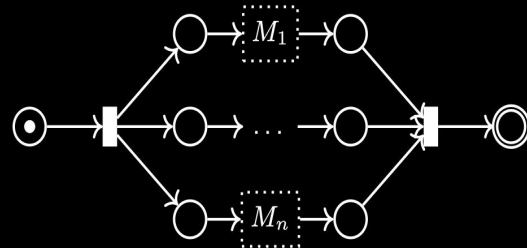
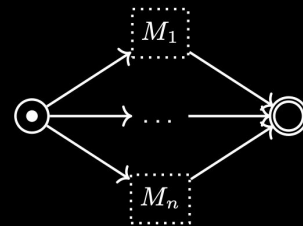
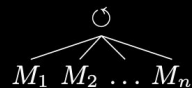
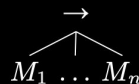
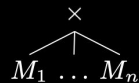
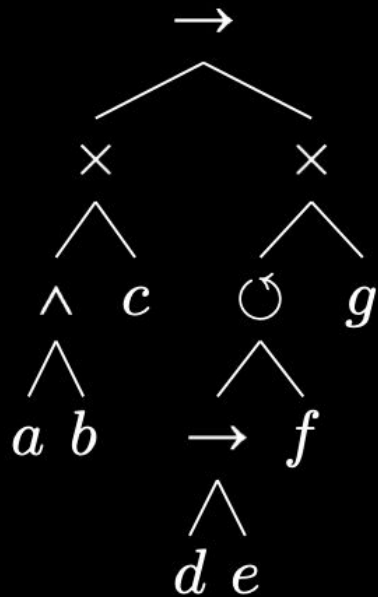
Definition 2.3 (workflow net). A workflow net is a Petri net (P, T, A, m_0, F, l) such that

- there is a single $i \in P$ such that $\bullet i = \emptyset$;
- there is a single $o \in P$ such that $o \bullet = \emptyset$;
- all places (P) and transitions (T) are on a path from i to o ;
- the initial marking consists of i : $m_0 = [i]$;
- the only final marking consists of o : $F = \{[o]\}$.

Definition 2.4 (soundness). Let $W = (P, T, A, [i], [o], l)$ be a workflow net, in which i is the source place and o is the sink place. W is sound if and only if:

- every transition can be fired, i.e. $\forall t \in T \exists [o] \rightsquigarrow_m \bullet t \subseteq m$;
- from every marking, reachable from $[i]$, it is possible to reach $[o]$, i.e. $\forall [i] \rightsquigarrow_m m \rightsquigarrow [o]$;
- every marking, reachable from $[i]$, that puts a token in o has no other tokens, i.e. $\forall [i] \rightsquigarrow_m o \in m \Rightarrow [o] = m$.

Process trees



Alpha algorithm example

<A, B, C>
<A, B, B, C>
<A, B, B, B, B, C>
<A, D, C>

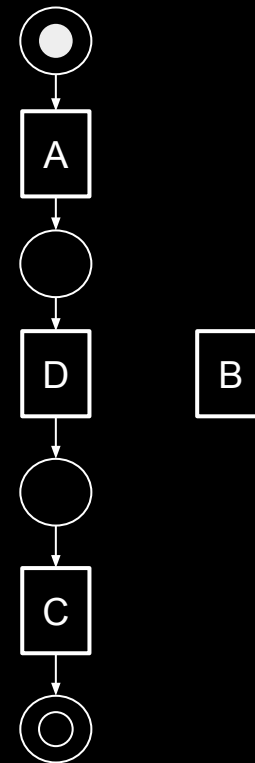
	A	B	C	D
A		3		1
B		3	3	
C				
D			1	

Directly follows relation
 $a \rightarrow b$

Parallel relation
 $a \rightarrow b \ \&\& \ b \rightarrow a$

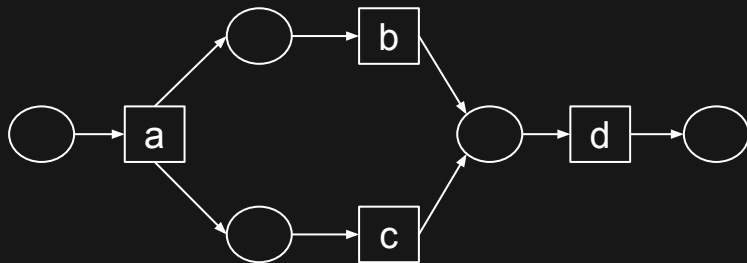
Causal relation
 $a \rightarrow b \ \&\& \ !(b \rightarrow a)$

Unrelated relation
 $!(a \rightarrow b) \ \&\& \ !(b \rightarrow a)$



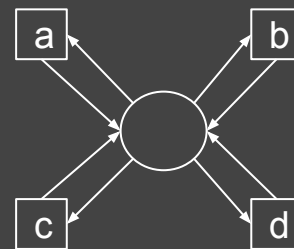
Fitness

fitness, precision, general, simple



Precision

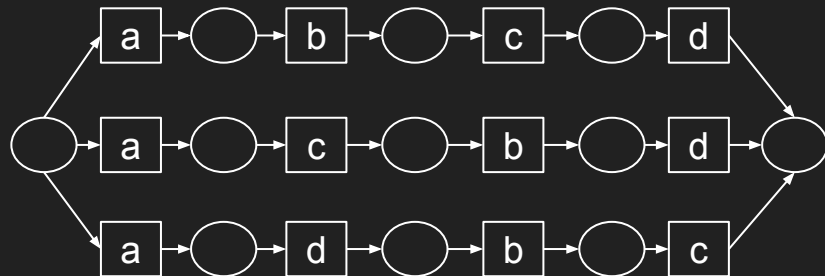
fitness, precision, general, simple



$[<a, b, c, d>^2, <a, c, b, d>^2, <a, d, b, c>]$

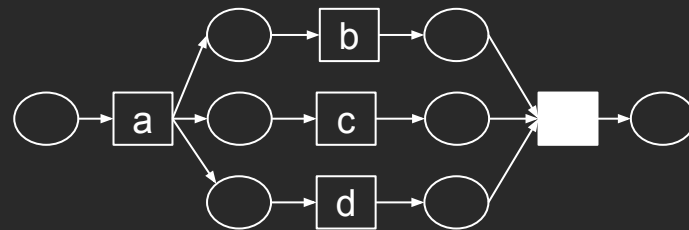
Simplicity

fitness, precision, general, simple



Generalization

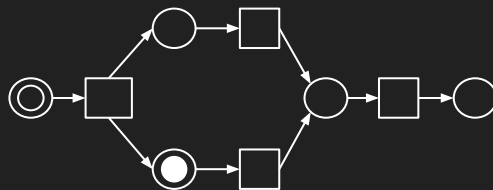
fitness, precision, general, simple



Naive approaches

Count the percentage of traces which fully fit the discovered model

Token replay game



P - produced tokens
C - consumed tokens
M - missing tokens
R - remaining tokens

$$\text{Fitness} = 0.5 * (1 - M/C) + 0.5 * (1 - R/P)$$

Alignments

Synchronous
move

Log	a	b	>>
Model	>>	b	c

Log
move

Model
move

$$\text{Fitness} = 1 - \text{alignment}/\text{worst_alignemnt}$$

Stream of events

$(e_{n-1}, t_{n-1}, c_{n-1}), (e_n, t_n, c_n), (e_{n+1}, t_{n+1}, c_{n+1})$

e - an event class

t - a timestamp of the event

c - case identifier

Stream of traces

A complete trace

T1 algorithms

(caching whole log + rediscover model each time)

<A, B, C>
<A, B, B, C>
<A, B, B, B, B, C>
<A, D, C>

Different caching strategies, i.e., strategy based on time, last updated trace, etc.

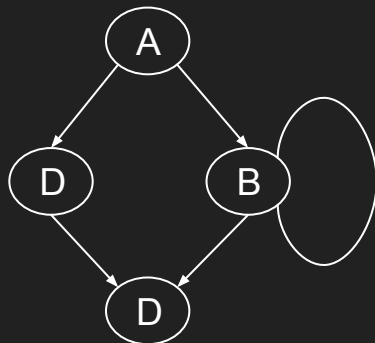
T2 algorithms

(online update of an abstraction + rediscovery each time)

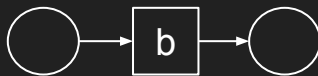
Events stream



Abstraction



Discovered model



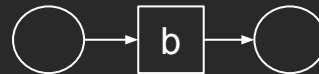
T3 algorithms

(incremental update of the discovered model)

Traces stream

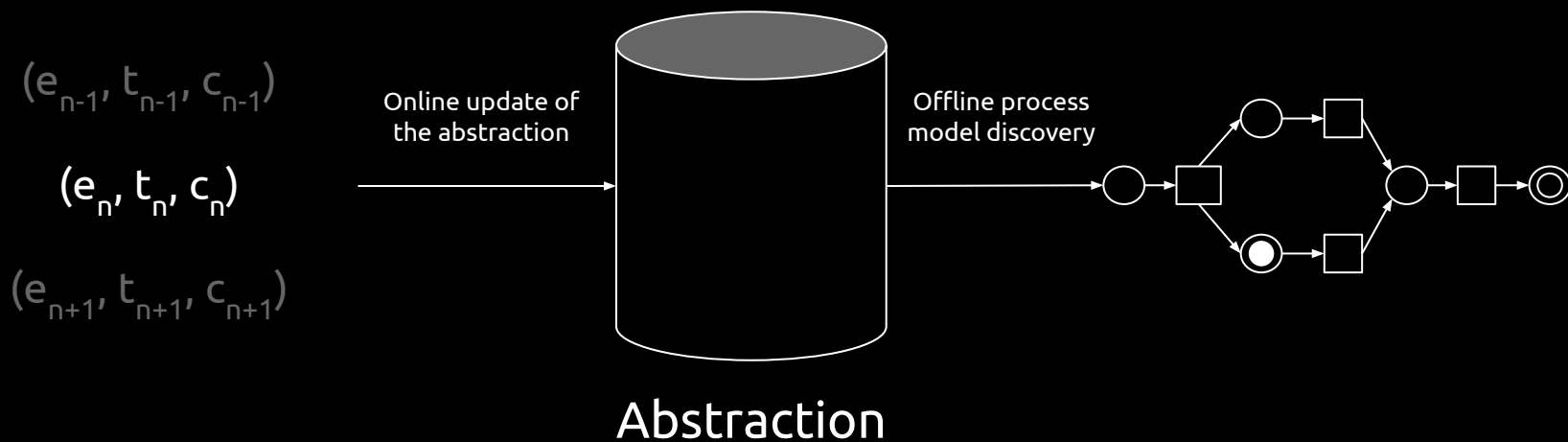


Discovered model



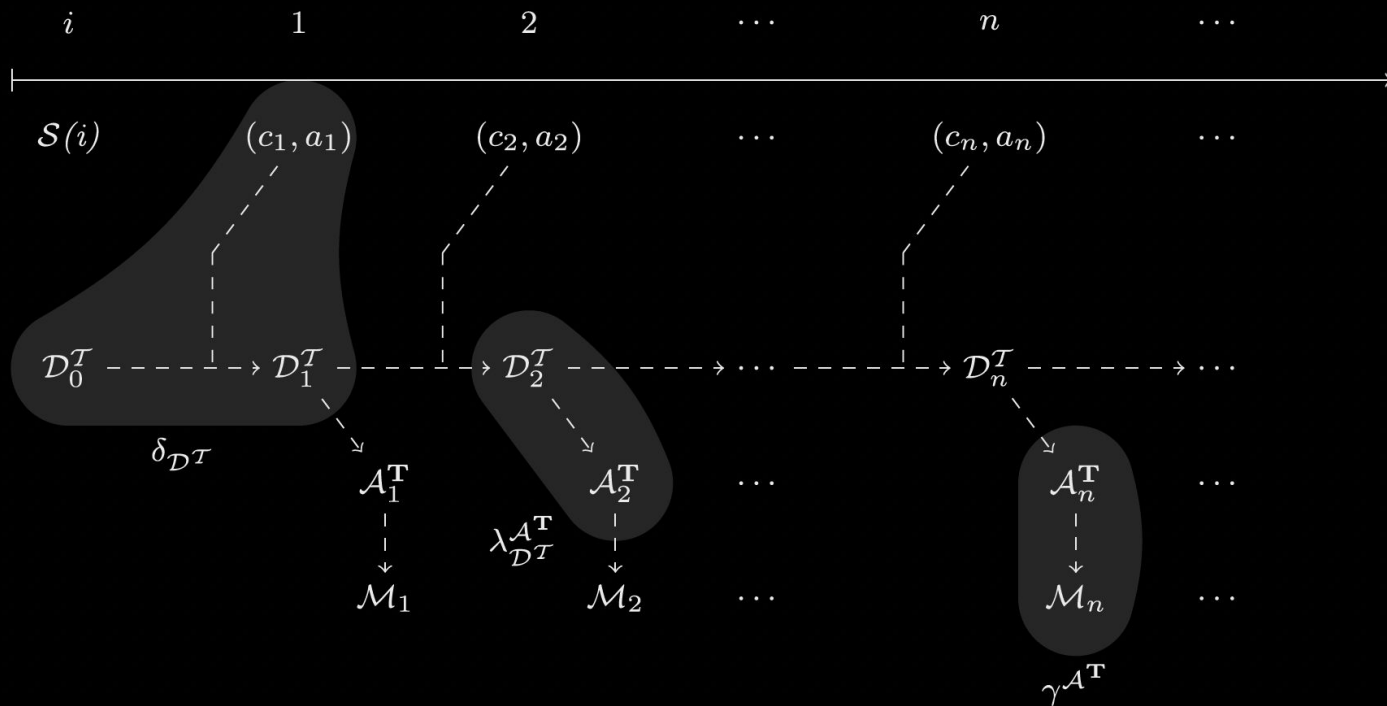
T2 Algorithms

S-BAR Architecture: concept



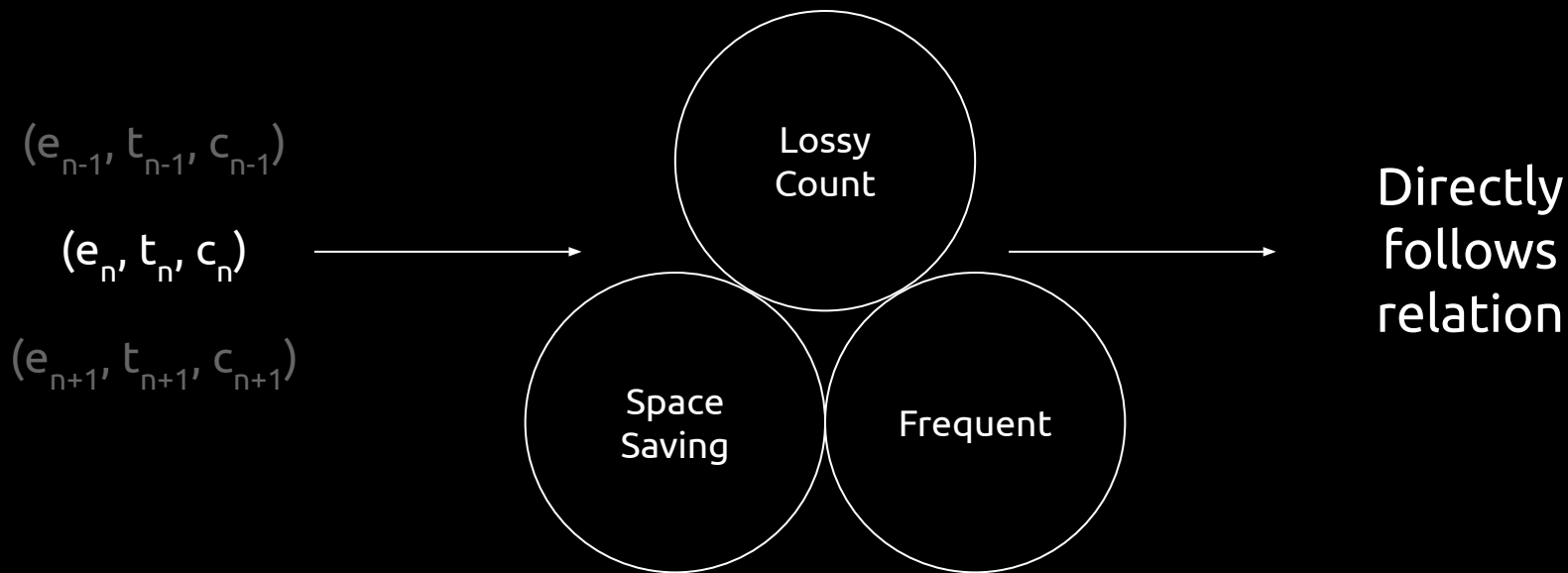
T2 Algorithms

S-BAR Architecture: formal description



T2 Algorithms

S-BAR Architecture: storing the abstraction



T2 Algorithms

S-BAR Architecture: Lossy Count and Frequent

Algorithm 2: $\mathcal{D}^C$ (Lossy)

```
input :  $k \in \mathbb{N}, \mathcal{S} \in (C \times A)^*, \mathcal{D}^A$ 
begin
1   $i, \Delta \leftarrow 0; X \leftarrow \emptyset;$ 
2  while true do
3       $i \leftarrow i + 1;$ 
4       $(c, a) \leftarrow \mathcal{S}(i);$ 
5      if  $\exists_{(c', a') \in X} (c' = c)$  then
6           $v_c \leftarrow v_c + 1;$ 
7           $\mathcal{D}^A \uplus \{(a', a)\};$ 
8           $X \leftarrow (X \cup \{(c, a)\}) \setminus \{(c, a')\};$ 
9      else
10          $X \leftarrow X \cup \{(c, a)\};$ 
11          $v_c \leftarrow \Delta;$ 
12     if  $\lfloor i/k \rfloor \neq \Delta$  then
13         foreach  $(c', a') \in X$  do
14             if  $v_{c'} \leq \Delta$  then
15                  $X \leftarrow X \setminus (c', a');$ 
16          $\Delta \leftarrow \lfloor i/k \rfloor;$ 
```

HashMap<String, String>

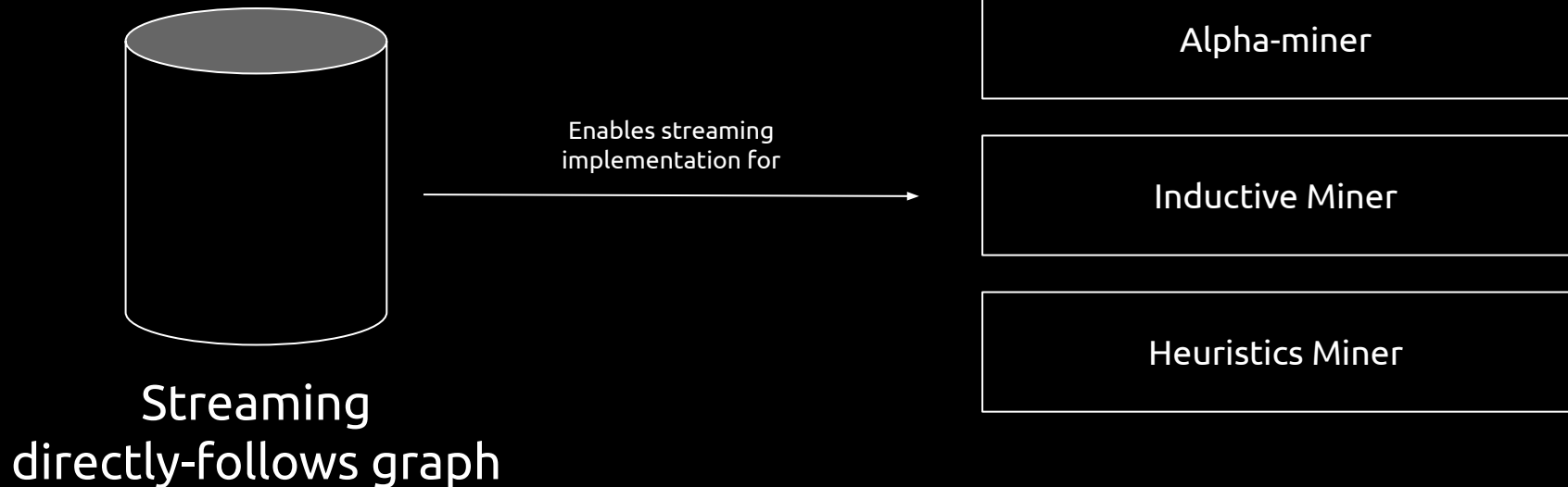
Algorithm 3: $\mathcal{D}^A$ (Frequent)

```
input :  $k \in \mathbb{N}, \mathcal{S}_A \in (A \times A)^*$ 
begin
1   $X \leftarrow \emptyset, i \leftarrow 0;$ 
2  while true do
3       $i \leftarrow i + 1;$ 
4       $(a, a') \leftarrow \mathcal{S}_A(i);$ 
5      if  $(a, a') \in X$  then
6           $v_{(a, a')} \leftarrow v_{(a, a')} + 1;$ 
7      else if  $|X| < k$  then
8           $X \leftarrow X \cup \{(a, a')\};$ 
9           $v_{(a, a')} \leftarrow 1;$ 
10     else
11         foreach  $(x, y) \in X$  do
12              $v_{(x, y)} \leftarrow v_{(x, y)} - 1;$ 
13             if  $v_{(x, y)} = 0$  then
14                  $X \leftarrow X \setminus \{(x, y)\};$ 
```

HashMap<(String, String), u64>

T2 Algorithms

S-BAR Architecture: Instantiations



T3 Algorithms

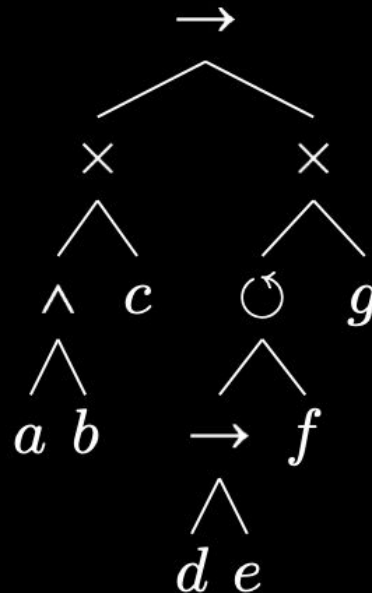
Incremental update of existing model

$\langle a, b, c, d, a, \dots \rangle$

$\langle a, b, c, d, a, b, d, c, \dots \rangle$

$\langle a, b, c, d, a, b, \dots \rangle$

Incremental update of process
trees, so that the model
matches new "event log"



T3 Algorithms

Example approach overview

Already discovered
process tree



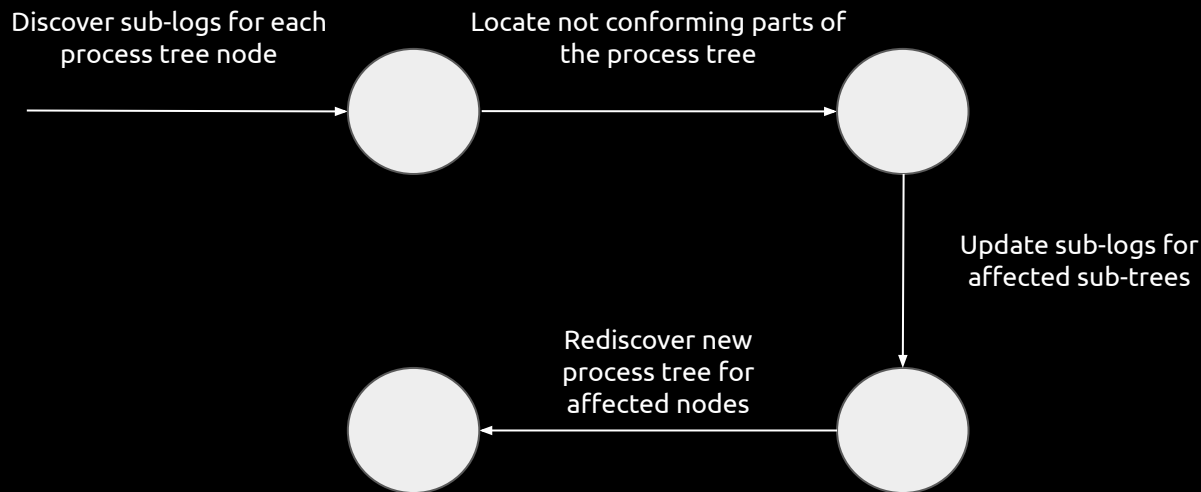
Existing
event log



New trace



Offline discovery
algorithms (IM)



T3 Algorithms

Example approach overview: creating sub-logs

Algorithm 1: Calculation of sub event logs for process trees

Input: $L \in \mathcal{B}(\mathcal{A}^*), T \in \mathcal{T}_{\mathcal{A}}$ (Assumption: $\{\sigma \in L\} \subseteq \mathcal{L}(T)$)

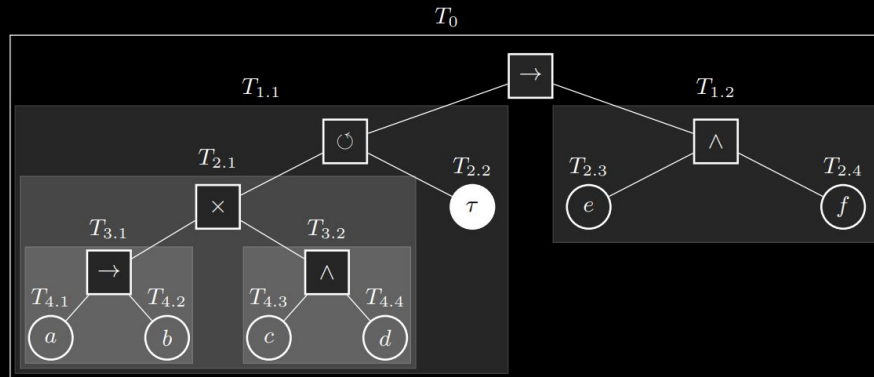
Output: sub event log for each subtree of T , i.e., $s: \mathcal{T}_{\mathcal{A}} \rightarrow \mathcal{B}(\mathcal{A}^*)$

begin

```

1  forall subtrees  $T'$  of  $T$  do
2     $s(T') \leftarrow []$  // initialize sub event logs
3  forall  $\sigma \in L$  do
4    let  $\gamma \in \bar{F}(\sigma, T)$  // calculate optimal alignment for  $\sigma$  and  $T$ 
5    forall subtrees  $T'$  of  $T$  do
6       $t(T') \leftarrow \langle \rangle$  // initialize trace for each subtree
7    for  $i \in \{1, \dots, |\gamma|\}$  do
8       $m \leftarrow \gamma(i)$  // extract  $i$ -th alignment move
9       $T_i \leftarrow \pi_2(m)$  // extract executed process leaf node
10   forall subtrees  $T'$  of  $T$  do
11     if  $T_i$  is subtree of  $T' \vee T_i = T'$  then
12        $t(T') \leftarrow t(T') \cdot \langle \pi_2(m) \rangle$  // add executed activity to  $T'$ 's trace
13     else if  $t(T') \neq \langle \rangle$  then
14        $s(T') \leftarrow s(T') \cup \{t(T')\}$  // add trace to  $T'$ 's sub event log
15        $t(T') \leftarrow \langle \rangle$  // reset trace
16  return  $s$ 

```



a	b	$\gg$	c	d	$\gg$	a	b	e	f
$(T_{4.1})$	$(T_{4.2})$	$(T_{2.2})$	$(T_{4.3})$	$(T_{4.4})$	$(T_{2.2})$	$(T_{4.1})$	$(T_{4.2})$	$(T_{2.3})$	$(T_{2.4})$
T_0	T_0		T_0	T_0		T_0	T_0	T_0	T_0
$T_{1.1}$	$T_{1.1}$		$T_{1.1}$	$T_{1.1}$		$T_{1.1}$	$T_{1.1}$		
$T_{2.1}$	$T_{2.1}$		$T_{2.1}$	$T_{2.1}$		$T_{2.1}$	$T_{2.1}$		
$T_{3.1}$	$T_{3.1}$		$T_{3.2}$	$T_{3.2}$		$T_{3.1}$	$T_{3.1}$		
								$T_{1.2}$	$T_{1.2}$

(a) Alignment and listing of subtrees containing the executed process tree leaf nodes

T_0	$[(a, b, c, d, a, b, e, f)]$
$T_{1.1}$	$[(a, b, c, d, a, b)]$
$T_{2.1}$	$[(a, b)^2, (c, d)]$
$T_{3.1}$	$[(a, b)^2]$
$T_{3.2}$	$[(c, d)]$
$T_{1.2}$	$[(e, f)]$

(b) Sub event logs

T3 Algorithms

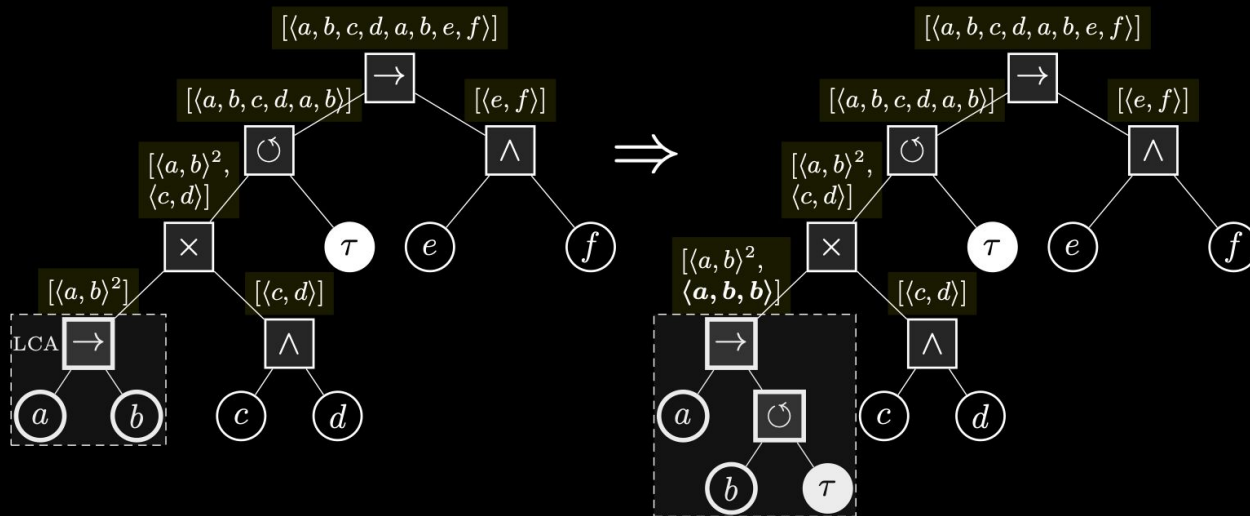
Example approach overview: locating deviations

$\dots$	x'_i	$\dots$	x_i	$\dots$	$\textit{deviation}(s)$	$\dots$	x_j	$\dots$	x'_j	$\dots$
$\dots$	T'_i	$\dots$	T_i	$\dots$	$\textit{deviation}(s)$	$\dots$	T_j	$\dots$	T'_j	$\dots$

T3 Algorithms

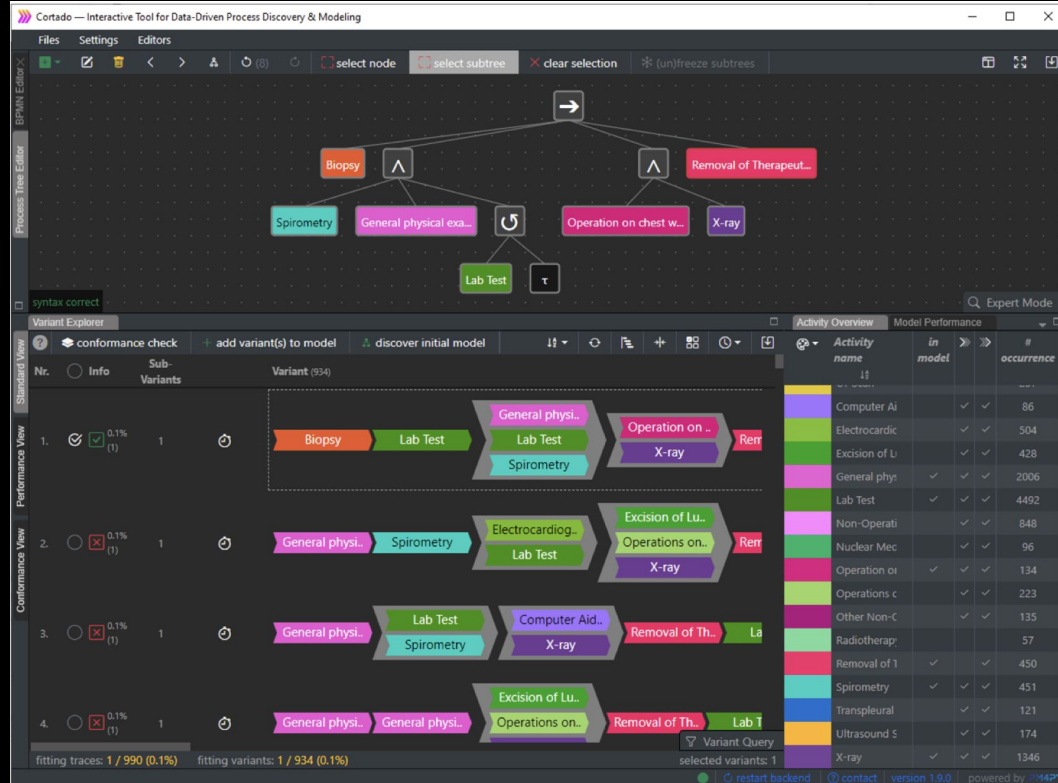
Example approach overview: repairing existing tree

New trace: $\langle a, b, b, e, f \rangle$



T3 Algorithms

Practical application: Cortado



Online Conformance Checking

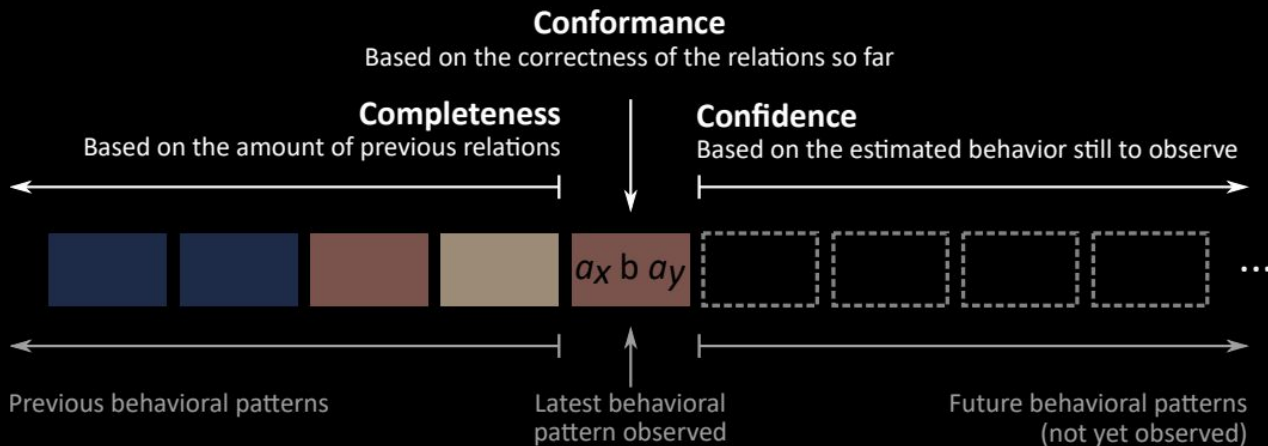
Incremental
computing of
prefix-alignments

Conformance
checking based on
behavioral patterns

Online Conformance Checking

Behavioral patterns

Definition 1 (Behavioural Pattern). Given a set of activities $\mathcal{A}$ and a set of possible control-flow relations $\mathcal{R}$, a behavioural pattern is defined as $b(a_1, a_2)$ where $a_1, a_2 \in \mathcal{A}$ are activities and $b \in \mathcal{R}$ represents a control-flow relation. An alternative writing of $b(a_1, a_2)$ is $a_1 \ b \ a_2$.



Online Conformance Checking

Behavioral patterns

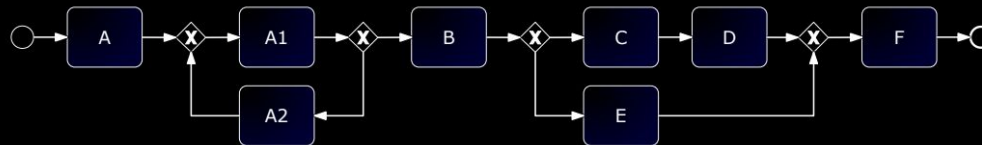


Fig. 1: Running example considered throughout this paper.

Table 1: Comparison of offline ([2]) and online conformance values (as proposed in this paper) based on the process model in Fig. 1.

Trace	Offline	Online		
	Conformance	Conformance	Completeness	Confidence
$t_1 = \langle A, A1, B, E, F \rangle$	1.00	1.00	1.00	1.00
$t_2 = \langle B, C, D, F \rangle$	0.78	1.00	0.60	1.00
$t_3 = \langle A, A1, A2, A1, B \rangle$	0.80	1.00	1.00	0.50
$t_4 = \langle B, C, D \rangle$	0.62	1.00	0.50	0.75

Online Conformance Checking

Behavioral patterns

Algorithm 1: Online conformance computation

Input: S : stream of behavioural patterns
 $M = (B, P, F)$: process model for online conformance

```

1 Initialize map obs           // Maps case ids to (finite) set of observed prescribed patterns
2 Initialize map inc           // Maps case ids to integers
3 forever do
4    $(c, b, t) \leftarrow \text{observe}(S)$            // New observable unit from the stream
   // Step 1: update internal data structures
5   if  $b \in B$  then
6      $\text{obs}(c) \leftarrow \text{obs}(c) \cup \{b\}$            // If  $b$  already in  $\text{obs}(c)$ , then no effect
7   else
8      $\text{inc}(c) \leftarrow \text{inc}(c) + 1$ 
   // Step 2: compute online conformance values
9    $\text{conformance}(c) \leftarrow \frac{|\text{obs}(c)|}{|\text{obs}(c)| + \text{inc}(c)}$ 
10  Notify new value of  $\text{conformance}(c)$ 
11  if  $b \in B$  then
12    if  $P_{\min}(b) \leq |\text{obs}(c)| \leq P_{\max}(b)$  then
13       $\text{completeness}(c) \leftarrow 1$ 
14    else
15       $\text{completeness}(c) \leftarrow \min \left\{ 1, \frac{|\text{obs}(c)|}{P_{\min}(b) + 1} \right\}$ 
16     $\text{confidence}(c) \leftarrow 1 - \frac{F(b)}{\max_{b' \in B} F(b')}$ 
17    Notify new values of  $\text{completeness}(c)$  and  $\text{confidence}(c)$ 
   // Step 3: cleanup
18   if size of obs and inc is close to max capacity then
19     Remove oldest entries from obs and inc

```

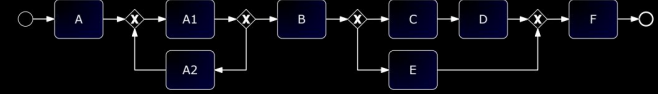


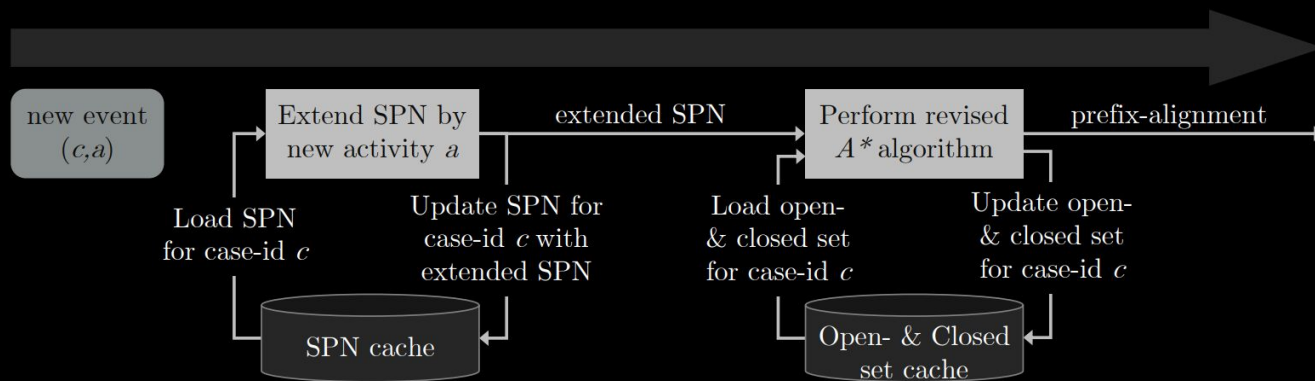
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$t_3 = \langle A, A1, A2, A1, B \rangle$	0.80	1.00	1.00	0.50
$t_4 = \langle B, C, D \rangle$	0.62	1.00	0.50	0.75

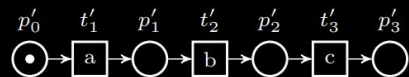
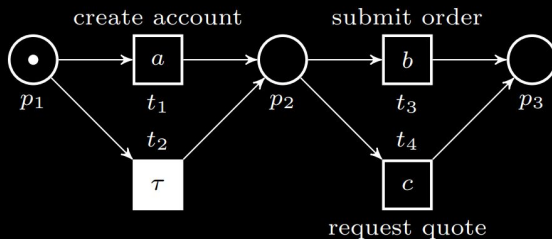
Online Conformance Checking

Prefix-alignments

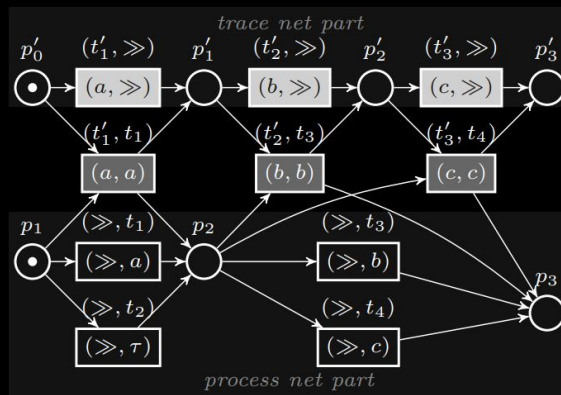


Online Conformance Checking

Prefix-alignments

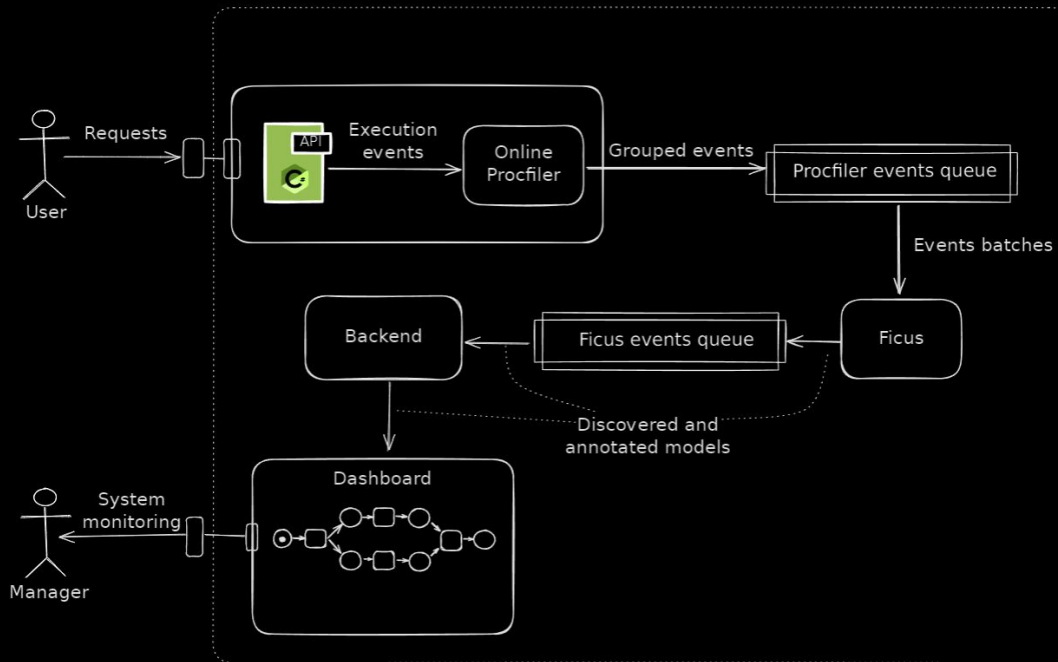


(a) Trace net of the trace $\langle a, b, c \rangle$



(b) SPN N_1^S of $\langle a, b, c \rangle$ and the WF-net N_1

The Need for Streaming Process Mining



Thanks for the
attention

References

Streaming Process Discovery

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